

Bridging Math Practices Math – Day 3

June 24, 2014

Goals for today

- *Understand what we mean by algebraic reasoning.*
- Recognize how different algebraic expressions connect to the problem at hand.
- *Analyze and evaluate understandings and/or misunderstandings on students' approaches to the hexagon task.*
- *Increase our understanding of the use of strip diagrams to solve different types of problems.*

Algebra and Algebraic Reasoning

"To think algebraically, one must be able to understand patterns, relations, and functions; represent and analyze mathematical situations and structures using algebraic symbols; use mathematical models to represent and understand quantitative relationships; and analyze change in various contexts."

(*Navigating through Algebra in Grades 3-5, NCTM, 2001*)

"Algebra and algebraic reasoning remain at the core of the high school mathematics curriculum. Algebra's dominance in the school curriculum is related to the importance of algebra in more advanced areas of mathematics, the usefulness of algebraic reasoning in all walks of life, and the role of algebra as a tool for the mathematical modeling required in many technological and scientific fields."

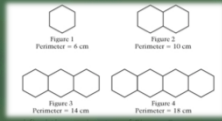
(*Focus in High School Mathematics: Reasoning and Sense Making, 2010, p. 1*)

Habits of Mind in Reasoning and Sense Making in Algebra

- **Analyzing a problem**, for example:
 - Defining relevant variables and conditions;
 - Seeking patterns and relationships;
 - Looking for hidden structure.
- **Implementing a strategy**, for example:
 - Making purposeful use of procedures;
 - Monitoring progress toward a solution.
- **Reflecting on a solution to a problem**, e.g.:
 - Interpreting a solution;
 - Considering the reasonableness of a solution;
 - Generalizing a solution to a broader class of problems;
 - Looking for connections to other problems.

Focus in High School Mathematics: Reasoning and Sense Making, 2010

Activity 1: Revisiting the Hexagon Task



- What is the perimeter of the 25th figure?
- Write a formula for the perimeter of the n -th figure.
- Analyze Student's work

Ratio: Two Perspectives

A COMPOSED UNIT/BATCH

Example: For every 7 female project participants in this room there is 1 male project participant.

Two quantities are in a ratio of A to B if for every A units present of the first quantity there are B units present of the second quantity.

FIXED NUMBERS OF PARTS

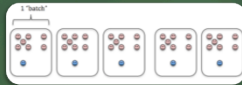
Example: Alvaro's favorite trail mix requires 1 parts of raisins, 4 parts granola, and 5 parts of M&M peanuts a bag/bowl.

Two quantities are in a ratio of A to B if we divide the first quantity into A equal parts, then the second quantity consist of B equal parts of the same size.

Ratio: Two Perspectives

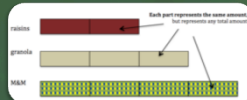
A COMPOSED UNIT/BATCH

Example: For every 7 female project participants in this room there is 1 male project participant.



FIXED NUMBERS OF PARTS

Example: Alvaro's favorite trail mix requires 2 parts of raisins, 4 parts granola, and 5 parts of M&M peanuts in each bowl.



Looking Back at Strip Diagrams

- Warm-Up Example:

The exchange rate of US Dollars and Euros is \$4 for €3. If a bottle of wine is €21, how much is the bottle in US Dollars?



Activity 2: Problem solving with Strip Diagrams

We will work on this in two groups

- One group stays here
 - 2nd- 5th grade teachers and math coaches
- Another group in Room 101
 - 6th grade – high school teachers

Guiding questions for reflection...

- What did we learn today?
 - Something old, new, borrowed?
- More specifically
 - What does it take to reason algebraically?
 - Any important results?
 - Take away from using strip diagrams on different problems
- Questions you still have
